

Honors Integrated Math III – Summer Math

Background: The exercises below cover concepts and skills that are pre-requisites for success in Honors Algebra 2. If you are unfamiliar with the content of any of these exercises, you may be at a disadvantage in the course. There will be a quiz on this material during the 2nd week of class.

1. **Evaluate** each expression below.

a. $(4053)^0$ b. $(-6)^2$ c. -6^2 d. $5^3 \div 2^5$

2. State an approximate value for each radical expression below.

a. $\sqrt{60}$ b. $\sqrt{15}$ c. $\sqrt{347}$

3. Classify each number below as rational (Q) or irrational (\bar{Q}). Explain your reasoning.

a. $\frac{10}{3}$ b. $\sqrt{5}$ c. π d. 0.8769

4. Explain the difference between the set of Integers (Z) and the set of Natural numbers (N).

5. Always, Sometimes, Never? $\frac{1}{3} = .33$

6. **Simplify** each expression below.

a. $(x+3)(x+2)$

f. $\sqrt{6} \cdot \sqrt{18}$

b. $(a-4)(a+6)$

g. $\frac{a^2b^4}{a^5b^3}$

c. $(3h+7)(h+9)$

h. x^2x^3

d. $(4n-10)(3n-1)$

i. $(x^2)^3$

e. $\sqrt{32} + \sqrt{18}$

7. **Solve** each equation and inequality below algebraically and graphically.

a. $2x+1=x$

c. $4(x-3)=x$

b. $5x-7 > 2x$

d. $6(x-5)=4(2x-1)$

8. **Factor** each expression below.

a. x^2-2x-3

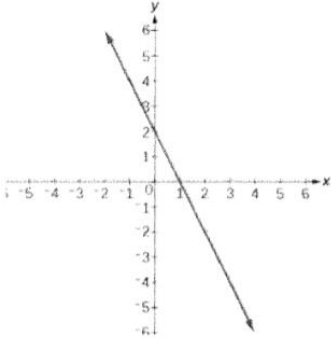
c. $4a^2-9$

b. $12x^2-11x-5$

d. $25x^2+10x+1$

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9. **Write an equation** for each situation described below. Then, identify both the x- and y-intercepts for each line.

<p>A – Write an equation in slope-intercept form for the line graphed below.</p>	<p>B</p>
	<p>Write an equation in point-slope form for the line that is perpendicular to the line on the right and passes through the point (3, 2).</p>
<p>C</p>	<p>D</p>
<p>Write an equation in point-slope form for the line that is parallel to the line above and passes through the point (-1, 3).</p>	<p>Write an equation in slope-intercept form for a line that passes through the points (3, 5) and (-2, 7).</p>

10. **Identify the solution** to the following system of inequalities:

$$x + y < 5$$

$$-\frac{1}{2}x + y > 1$$

11. **Write an equation** to represent each situation described below.

- a. Maria currently has 200 songs in her music collection. Starting in January, at the end of every month, she adds 15 new songs.
 - i. Write a formula for the number of songs, N , in her collection as a function of time, t , where $t = \#$ of months after December 31.
 - ii. How many songs will Maria have at the beginning of September?
- b. Kim sells necklaces to earn spending money. From past experience, she knows that if she charges \$20 per necklace, she will sell about 12 necklaces per week. If she raises her price to \$25, her weekly sales will fall to 10 necklaces per week.
 - i. Build a linear function in slope-intercept form to model the number of necklaces that Kim can sell as a function of price. Define all variables, including units.
 - ii. What is the slope of your function? What does the slope value mean in this particular context?

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- c. The number of rats in a particular rat population is shown below. Let w = # of weeks and r = # of rats.

# weeks	0	2	4	6
# rats	400	480	560	640

- Describe in words how the population is changing over time.
- Write a formula to model how the population is changing over time.
- If this trend continues, what would the population be in Week 15?

Answers:

1. Evaluate each expression below.

a. $(4053)^0 = 1$

d. $5^3 \div 2^5 = \frac{125}{32}$ or 3.90625

b. $(-6)^2 = 36$

c. $-6^2 = -36$

2. State an approximate value for each radical expression below.

a. $\sqrt{60}$ between 7 and 8, closer to 8

c. $\sqrt{347}$ between 18 and 19

b. $\sqrt{15}$ between 3 and 4, closer to 4

3. Classify each number below as rational (Q) or irrational (\bar{Q}). Explain your reasoning.

a. $\frac{10}{3}$ rational

c. π irrational

b. $\sqrt{5}$ irrational

d. 0.8769 rational

4. Explain the difference between the set of Integers (Z) and the set of Natural numbers (N).

The set of Natural numbers is a subset of the set of Integers. It includes only the positive integers.

5. Always, Sometimes, Never? $\frac{1}{3} = .33$ NEVER, $\frac{1}{3}$ is an exact value; 0.33 is only an approximation

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6. **Simplify** each expression below.

a. $(x+3)(x+2) = x^2 + 5x + 6$

f. $\sqrt{6} \cdot \sqrt{18} = \sqrt{108} = 6\sqrt{3}$

b. $(a-4)(a+6) = a^2 + 2a - 24$

g. $\frac{a^2b^4}{a^5b^3} = \frac{b}{a^3}$

c. $(3h+7)(h+9) = 3h^2 + 34h + 63$

h. $x^2x^3 = x^5$

d. $(4n-10)(3n-1) =$

$12n^2 - 34n + 10$

i. $(x^2)^3 = x^6$

e. $\sqrt{32} + \sqrt{18} =$

$4\sqrt{2} + 3\sqrt{2} = 7\sqrt{2}$

7. **Solve** each equation and inequality below algebraically and graphically.

a. $2x+1 = x \rightarrow x = -1$

c. $4(x-3) = x \rightarrow x = 4$

b. $5x-7 > 2x \rightarrow x > \frac{7}{3}$

d. $6(x-5) = 4(2x-1) \rightarrow x = -13$

8. **Factor** each expression below.

a. $x^2 - 2x - 3 = (x-3)(x+1)$

c. $4a^2 - 9 = (2a+3)(2a-3)$

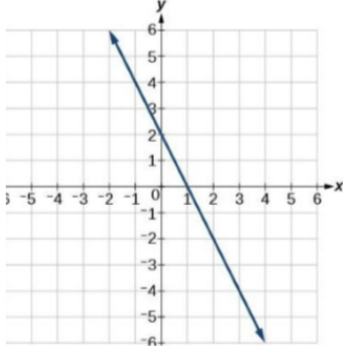
b. $12x^2 - 11x - 5 =$

$(4x-5)(3x+1)$

d. $25x^2 + 10x + 1 = (5x+1)^2$

9. **Write an equation** for each situation described below. Then, identify both the x- and y-intercepts for each line.

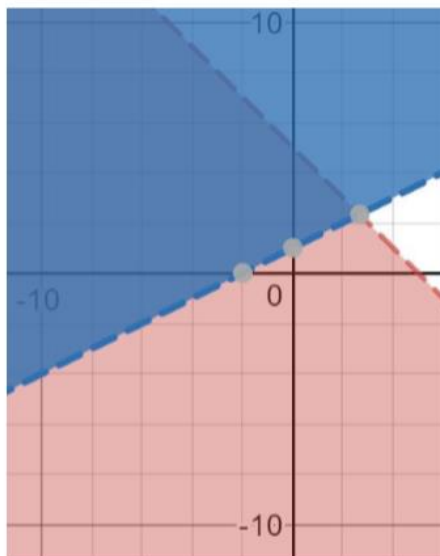
Write an equation in slope-intercept form for the line graphed below.	B
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	<p>Write an equation in point-slope form for the line that is perpendicular to the line on the right and passes through the point (3, 2).</p>
$y = -2x + 2$	$(y - 2) = \frac{1}{2}(x - 3)$
<p style="text-align: center;">C</p>	<p style="text-align: center;">D</p>
<p>Write an equation in point-slope form for the line that is parallel to the line above and passes through the point (-1, 3).</p>	<p>Write an equation in slope-intercept form for a line that passes through the points (3, 5) and (-2, 7).</p>
$y = -2x + 1$	$y = -\frac{2}{5}x + \frac{31}{5}$

10. Identify the solution to the following system of inequalities:

$$\begin{aligned} x + y &< 5 \\ -\frac{1}{2}x + y &> 1 \end{aligned}$$

Answer: The darkest shaded area below between the dotted lines.



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11. **Write an equation** to represent each situation described below.

- a. Maria currently has 200 songs in her music collection. Starting in January, at the end of every month, she adds 15 new songs.

i. Write a formula for the number of songs, N , in her collection as a function of time, t , where t = # of months after December 31.

Answer: $N = 200 + 15t$

ii. How many songs will Maria have at the beginning of September?

Answer: Maria will have 320 songs at the beginning of September

- b. Kim sells necklaces to earn spending money. From past experience, she knows that if she charges \$20 per necklace, she will sell about 12 necklaces per week. If she raises her price to \$25, her weekly sales will fall to 10 necklaces per week.

i. Build a linear function in slope-intercept form to model the number of necklaces that Kim can sell as a function of price. Define all variables, including units.

Let y = # of necklaces Kim sells per week and x = price per necklace (in \$)

Answer: $y = -\frac{2}{5}x + 20$

ii. What is the slope of your function? What does the slope value mean in this particular context?

Answer: slope = $-\frac{2}{5}$ or -0.4

Meaning: On average, every \$5 increase in price reduces weekly sales by 2 necklaces.

- c. The number of rats in a particular rat population is shown below. Let w = # of weeks and r = # of rats.

# weeks	0	2	4	6
# rats	400	480	560	640

i. Describe in words how the population is changing over time.

Answer: On average, the population increases by 40 rats per week.

ii. Write a formula to model how the population is changing over time.

Answer: $r = 400 + 40w$

iii. If this trend continues, what would the population be in Week 15?

Answer: If this trend continues, there will be 1000 rats in Week 15.